

D.K.M.COLLEGE FOR WOMEN (AUTONOMOUS),VELLORE-1.

NUMERICAL METHODS

UNIT – I SECTION-A (2 MARKS)

1. Define transcendental equation.
2. What is Bisection method?
3. Explain Regular falsie method
4. Define newton raphson method
5. Find the square root of 20
6. What is generalized hewton – Raphson method?

SECTION-B 10 Marks

1. Find the Positive root of $x^4 - x^3 - 2x^2 - 6x - 4 = 0$ correct to 4 decimal places by bisection method.
2. Solve the equation $x^3 - 9x + 1 = 0$ for the root lies between 2 and 3.
3. Solve the equation $x^3 - 4x + 1 = 0$, by regular falsi method.
4. Find the root of $x^3 - x - 1 = 0$ by newton's method.
5. Find a double root of the equation $x^3 - x^2 - x + 1 = 0$ and the root is nearer to 0.8

UNIT – II SECTION-A (2 marks)

1. Explain the forward difference formula.
2. Explain the backward difference formula.
3. Prove that $\mu = \frac{1}{2} [E^{\frac{1}{2}} + E^{-\frac{1}{2}}]$
4. P.T $s = E^{\frac{1}{2}} - E^{-\frac{1}{2}}$
5. P.T (i) $\nabla = 1 - E^{-1}$, (ii) $ke^2 = 1 + s^2 / 4$
6. If

x	10	15	20	25	30	35
y	19.97	21.51	22.57	23.52	24.65	25.89

Form the difference table and find value of $\Delta^2 y_{10}$, Δy_{20} , $\Delta^3 y_{15}$, $\Delta^5 y_{10}$.

7. Define Lagrange's Interpolation Formula For unequed intervals,
8. Define inverse interpolation formula.
9. prove the Δ is linear.
10. Explain newton's general interpolation formula.

SECTION-B (10marks)

1. Estimate the population 1964 and 1966 form the following data.

year	1961	1962	1963	1964	1965	1966	1967
production	200	200	260		350		430

2. From the following data find θ at $x=43$, $x=84$

x	40	50	60	70	80	90
θ	184	204	226	250	276	304

3. use largrange's interpolation formula find y (10) for the following data

x	5	6	9	11
y	12	13	14	16

4. using newtons divided different formula find the value of $f(2)$, $f(8)$, & $f(15)$

x	4	5	7	10	11	13
f(x)	48	100	294	900	1210	2028

UNIT-III SECTION-A (2 marks)

1. Explain newton's Forward difference interpolation formula.
2. Explain newton's backward difference interpolation formula.
3. Derive Simpsons one third rule.
4. Derive trapezoided rule.

SECTION-B (10 marks)

1. from the following values of x & y obtain $dy/dx, d^2y/dx^2$ for $x=1.2$ and $x=2.2$

x	1.0	1.2	1.4	1.6	1.8	2.0	2.2
y	2.7183	3.3201	4.0552	4.9530	6.0496	7.3891	9.0250

2. Evaluate $\int_{-3}^3 x^2$ taking 6 interval using
3. (1) Trapezoidal rule (2) simpson's 1/3 rd rule (3) Simpson's 3/8 the rule. Find the minimum value of f(x) which has values

x	0	2	4	6
f(x)	3	3	11	27

UNIT-IV SECTION-A (2 marks)

1. Derive Gauss Elimination method.
2. define factorization method.

(10marks)

1. Solve by Gauss Elimination method.
 $3x+2y+4z=7, 2x+y+z=7, x+3y+5z=2.$
2. Solve the Equations by Factorization method .
 $2x+3y+z=9, x+2y+3z=6, 3x+y+2z=8$

UNIT-V SECTION-A (2 marks)

1. Derive Taylor's formula.
2. What is Picard's method.
3. Derive Euler's method.
4. Explain Runge-Kutta method

SECTION-B (10 Marks)

1. Using Taylor's method, compute $y(0.2)$ and $y(0.4)$ correct to 4 decimal places given $\frac{dy}{dx} = 1-2xy$ and $y(0)=0.1$
2. Given $\frac{dy}{dx} = x^3+y$, $y(0)=2$, compute $y(0.2), y(0.4), y(0.6)$ by Runge-kutta method of order two.