

## PROBABILITY THEORY

| Semester | Subject Code | Category         | Lecture  |         | Theory   |         | Practical | Credits |
|----------|--------------|------------------|----------|---------|----------|---------|-----------|---------|
| III      | 21CPMA3D     | Core – Paper XII | Hrs/week | Hrs/Sem | Hrs/week | Hrs/Sem | 0         | 5       |
|          |              |                  | 6        | 90      | 6        | 90      |           |         |

### COURSE OBJECTIVES:

The students will be able to

- Understand axiomatic approach to probability theory
- Study some statistical characteristics, discrete and continuous distribution functions and their properties, characteristic function and basic limit theorems of probability.

### COURSE OUTCOMES:

On the successful completion of the course, the students will be able to

| CO Number | CO Statement  | Knowledge Level (K1-K4) |
|-----------|---|-------------------------|
| CO1       | Understand the important concepts of the random experiments.  | K2                      |
| CO2       | Explain about the properties of characteristic function and find distribution function by the characteristic function.                                    | K3                      |
| CO3       | Examine a random variable or to characterize its distribution by a few parameters of the random variable.   | K3                      |
| CO4       | Apply discrete and continuous distributions in detail that plays an important role in many engineering applications as special probability distributions. | K3                      |
| CO5       | Learn the concept of convergence in probability and prove naming theorems for independently and identically distributed random variables                  | K4                      |

*Knowledge Level: K1 – Remember; K2 – Understand; K3 – Apply; K4 – Analyze.*

### MAPPING WITH PROGRAM ME OUTCOMES

| COS | PO1 | PO2 | PO3 | PO4 | PO5 | PO6 |
|-----|-----|-----|-----|-----|-----|-----|
| CO1 | S   | S   | M   | M   | M   | S   |
| CO2 | S   | M   | S   | M   | M   | S   |
| CO3 | S   | S   | M   | M   | S   | S   |
| CO4 | S   | M   | S   | S   | M   | S   |
| CO5 | S   | S   | M   | M   | M   | S   |

S- Strong; M – Medium; L – Low

**UNIT- I: RANDOM EVENTS AND RANDOM VARIABLES****18 Hours**

Random events – Probability axioms – Combinatorial formulae – conditional probability – Bayes Theorem – Independent events – Random Variables – Distribution Function – joint Distribution – Marginal Distribution – Conditional Distribution - Independent random variables – Functions of multi dimensional random variables.

**Chapter 1: Sections 1.1 to 1.7****Chapter 2: Sections 2.1 to 2.9****UNIT- II: PARAMETERS OF THE DISTRIBUTION****18 Hours**

Expectation – Moments – The Chebyshev's Inequality – Absolute moments – Order parameters – Moments of random vectors – Regression of the first and second types.

**Chapter 3: Sections 3.1 to 3.8****UNIT-III: CHARACTERISTIC FUNCTIONS****18 Hours**

Properties of characteristic functions – Characteristic functions and moments – semi – invariants – characteristic function of the sum of the independent random variables –Determination of distribution function by the Characteristic function – Characteristic function of multidimensional random vectors – Probability generating functions

**Chapter 4: Sections 4.1 to 4.7****UNIT- IV: SOME PROBABILITY DISTRIBUTIONS****18 Hours**

One point, two point, Binomial – Polya –Hypergeometric – Poisson [discrete ] distributions – Uniform – normal gamma – Beta – Cauchy and Laplace [continuous] distributions.

**Chapter 5: Section 5.1 to 5.10****UNIT-V: LIMIT THEOREMS****18 Hours**

Stochastic convergence – Bernoulli law of large numbers – Convergence of sequence of distribution functions – Levy-Cramer Theorems – De Moivre Laplace theorem – Poisson, Chebyshev, Khintchine Weak law of large numbers –Lindberg Theorem –Lyapunov theorem- Borel-Cantelli Lemma – Kolmogorov Inequality and Kolmogorov Strong law of large numbers

**Chapter 6: Sections 6.1 to 6.4, 6.6 to 6.9, 6.11 and 6.12 [omit sections 6.5, 6.10, 6.13 to 6.15]**

## **DISTRIBUTION OF MARKS: THEORY 80% AND PROBLEMS 20%**

### **TEACHING METHODOLOGY**

1. Class room teaching
2. Giving Assignments for all units
3. Discussions
4. Home test
5. PPT presentation

### **TEXT BOOK**

| <b>S.NO</b> | <b>AUTHORS</b> | <b>TITLE</b>                                   | <b>PUBLISHERS</b>             | <b>YEAR OF PUBLICATION</b> |
|-------------|----------------|--|-------------------------------|----------------------------|
| 1.          | MarekFisz      | Probability Theory and Mathematical Statistics | John Wiley and Sons, New York | 1963                       |

### **REFERENCE BOOKS:**

| <b>S.NO</b> | <b>AUTHORS</b> | <b>TITLE</b>   | <b>PUBLISHERS</b>                        | <b>YEAR OF PUBLICATION</b> |
|-------------|----------------|--|--|----------------------------|
| 1.          | R.B. Ash       | Real Analysis and probability  | Academic Press, New York                 | 1972                       |
| 2.          | K.L.Chung      | A Course in Probability  | Academic Press, New York                 | 1974                       |
| 3.          | R.Durrett      | Probability Theory and Examples [2 <sup>nd</sup> Edition]                                | Duxbury press, New York                  | 1996                       |
| 4.          | V.K. Rohatgi   | An Introduction to Probability Theory and Mathematical Statistics[3 <sup>rd</sup> print] | Wiley Eastern Ltd., New Delhi            | 1988                       |
| 5.          | S.I.Resnick    | A Probability Path   | Birhauser, Berlin                        | 1999                       |
| 6.          | B.R. Bhat      | Modern Probability Theory [3 <sup>rd</sup> Edition]                                      | New Age International [P] Ltd, New Delhi | 1999                       |

### **WEB SOURCES:**

1. [www.researchgate.net/publication/272237355\\_probability\\_and\\_mathematical\\_statistics.pdf](http://www.researchgate.net/publication/272237355_probability_and_mathematical_statistics.pdf)
2. [www.freebookcentre.net/Mathematics/Probability-Theory-Book.html](http://www.freebookcentre.net/Mathematics/Probability-Theory-Book.html)

### **SYLLABUS DESIGNER**

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